## B. P. PODDAR IN STITUTE OF MANAGEMENT AND TECHNOLOGY DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING ACADEMIC YEAR: 2021-22

## COURSE OUTCOMES

Course:Design and Analysis of Algorithms<br>Code: PCC-CS404<br>Branch \& Sec: CSE (Sec-B)

## COURSE OUTCOMES:

| Sl No | Course Outcomes | Cognitive Level | PO mapping | PSO mapping |
| :---: | :---: | :---: | :---: | :---: |
| CS404.1 | Able to Argue the correctness of algorithms using inductive proofs and Analyze worst-case running times of algorithms using asymptotic analysis. | Analyze | $\begin{gathered} \hline \text { PO1, PO2, } \\ \text { PO3, PO4, } \\ \text { PO8, PO9, } \\ \text { PO10 } \\ \hline \end{gathered}$ | PSO1,PSO2 |
| CS404.2 | Able to explain important algorithmic design paradigms (divide-and-conquer, greedy method, dynamic-programming and Backtracking) and apply when an algorithmic design situation calls for it. | Create | $\begin{aligned} & \begin{array}{l} \text { PO1, PO2, } \\ \text { PO3, PO4, } \\ \text { PO8, PO9, } \\ \text { PO10, PO12 } \end{array} \end{aligned}$ | PSO1,PSO2 |
| CS404.3 | Able to Explain the major graph algorithms and Employ graphs to model engineering problems, when appropriate. | Create | $\begin{gathered} \text { PO1, PO2, } \\ \text { PO3, PO4, } \\ \text { PO8, PO9, } \\ \text { PO10,, PO12 } \end{gathered}$ | PSO1,PSO2 |
| CS404.4 | Able to Compare between different data structures and pick an appropriate data structure for a design situation | Analyze | $\begin{aligned} & \hline \text { PO1, PO2, } \\ & \text { PO3, PO4, } \\ & \text { PO8, PO9, } \\ & \text { PO10, PO12 } \\ & \hline \end{aligned}$ | PSO1,PSO2 |
| CS404.5 | Able to Describe the classes P, NP, and NPComplete and be able to prove that a certain problem is NP-Complete. | Evaluate | $\begin{gathered} \text { PO1, PO2, } \\ \text { PO3, PO4, } \\ \text { PO8, PO9, } \\ \text { PO10 } \end{gathered}$ | PSO1,PSO2 |
| CS404.6 | Able to perform Amortized analysis for data structures like Hash Tables, Disjoint Sets and Splay Trees. | Analyze | PO1, PO2, <br> PO3, PO4, <br> P08, P09, <br> PO10 | PSO1,PSO2 |

## CO MAPPING WITH PO/PSO

## Course: Design and Analysis of Algorithms

Code: PCC-CS404
Branch \& Sec: Computer Science \& Engineering (Sec-B)

## COURSE OUTCOMES VS PO and PSO MAPPING:

|  | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | PO8 | PO9 | PO10 | PO11 | PO12 | PSO1 | PSO2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { PCCCS } \\ 404.1 \\ \hline \end{gathered}$ | 2 | 3 | 2 | 2 | - | - | - | 1 | 1 | 2 | - | - | 2 | 2 |
| $\begin{gathered} \text { PCCCS } \\ 404.2 \\ \hline \end{gathered}$ | 3 | 3 | 3 | 2 | - | - | - | 1 | 1 | 2 | - | 3 | 2 | 2 |
| $\begin{gathered} \text { PCCCS } \\ 404.3 \\ \hline \end{gathered}$ | 2 | 3 | 3 | 3 | - | - | - | 1 | 1 | 2 | - | 3 | 2 | 2 |
| $\begin{gathered} \text { PCCCS } \\ 404.4 \\ \hline \end{gathered}$ | 2 | 3 | 2 | 2 | - | - | - | 1 | 1 | 2 | - | 3 | 2 | 2 |
| $\begin{gathered} \text { PCCCS } \\ 404.5 \\ \hline \end{gathered}$ | 2 | 3 | 2 | 3 | - | - | - | 1 | 1 | 2 | - | - | 2 | 2 |
| $\begin{gathered} \hline \text { PCCCS } \\ 404.6 \\ \hline \end{gathered}$ | 2 | 3 | 2 | 3 | - | - | - | 1 | 1 | 2 | - | - | 2 | 2 |
| $\begin{gathered} \text { PCCCS4 } \\ 04 \\ \hline \end{gathered}$ | 2.2 | 3 | 2.3 | 2.5 | - | - | - | 1 | 1 | 2 | - | 3 | 2 | 2 |

For Entire Course, PO/PSO Mapping; 1 (Low); 2 (Medium); 3 (High) Contribution to PO/PSO

## PO REFERENCE:

| P01+ | Engineering†Knowle dget | $\begin{array}{\|l} \hline \mathrm{PO} \\ \text { t } \\ \hline \end{array}$ | Environment+\& $\dagger$ Sustainabi lityt | $\begin{array}{\|l\|} \hline \text { PSO1 } \\ + \\ \hline \end{array}$ | $\begin{array}{\|l} \hline \text { Domain+Skills } \\ 1 \dagger \\ \hline \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PO2† | Problem†Analysis $\dagger$ | $\begin{aligned} & \hline \text { PO8 } \\ & t \\ & \hline \end{aligned}$ | Ethics $\dagger$ | $\begin{array}{\|l\|} \hline \text { PSO2 } \\ \dagger \\ \hline \end{array}$ | $\begin{aligned} & \begin{array}{l} \text { Domain+Skills } \\ 2 \dagger \end{array} \\ & \hline \end{aligned}$ |
| PO3t | Designt\& $\dagger$ Developme nt $\dagger$ | $\begin{aligned} & \mathrm{PO9} \\ & \mathrm{t} \\ & \hline \end{aligned}$ | Individualt\&†Team†Wo rk $\dagger$ | $\dagger$ | $\dagger$ |
| P04 | Investigations $\dagger$ | $\begin{aligned} & \hline \text { P010 } \\ & t \end{aligned}$ | Communication†Skills $\dagger$ | $\dagger$ | $\dagger$ |
| P05 | Modern†Tools $\dagger$ | $\begin{array}{\|l\|} \hline \text { P011 } \\ \dagger \\ \hline \end{array}$ | $\underset{\text { e } \dagger}{\text { Project } \dagger \text { Mgt. } \dagger \& \dagger \text { Financ }}$ | $\dagger$ | $\dagger$ |
| P06 | Enginerrt\& $\dagger$ Societ <br> y $\dagger$ | $\begin{aligned} & \hline \mathrm{PO12} \\ & \dagger \\ & \hline \end{aligned}$ | Life†Long†Learning $\dagger$ | $\dagger$ | $\dagger$ |

## $\dagger$

PSO REFERENCE:

| PSO1 | Students will have proficiency in emerging domains like artificial <br> intelligence, data science and distributed computing to develop <br> solutions through innovative projects and research. |
| :--- | :--- |
| PSO2 | Students will have capabilities to work in synergized teams to cater <br> to the dynamic needs of the industry and society. |

## JUSTIFICATION FOR MAPPING:

| CO | PO MAPPED | LEVEL | JUSTIFICATION |
| :---: | :---: | :---: | :---: |
| PCCCS404.1 | PO1, PO2, PO3, PO4, PO8, PO9, PO10 | $\begin{array}{lll} 2, & 3, & 2, \\ 2, & 1, & 1, \\ 2 & \end{array}$ | This is highly correlated with engineering knowledge and problem analysis since it deals with correctness and running time of algorithms. |
| PCCCS404.2 | PO1, <br> PO2, <br> PO3, <br> PO4, <br> PO8, <br> PO9, <br> PO10, PO12 | $\begin{array}{lll} 3, & 3, & 3, \\ 2, & 1, & 1, \\ 2,3 \end{array}$ | Most importantly this is the main CO in Design and Analysis of Algorithm course by providing the different design techniques to develop an efficient algorithms |
| PCCCS404.3 | $\begin{aligned} & \text { PO1, } \\ & \text { PO2, } \\ & \text { PO3, } \\ & \text { PO4, } \\ & \text { PO8, } \\ & \text { PO9, } \\ & \text { PO10, PO12 } \end{aligned}$ | $\begin{aligned} & 2,3,3, \\ & 3,1,1, \\ & 2,3 \end{aligned}$ | Essentially this CO relates to different graph traversal algorithms which are used for social network analysis and our day to day problem. |
| PCCCS404.4 | $\begin{aligned} & \text { PO1, PO2, } \\ & \text { PO3, PO4, } \\ & \text { PO8, PO9, } \\ & \text { PO10, PO12 } \end{aligned}$ | $\begin{aligned} & 2,3,2, \\ & 2,1,1, \\ & 2,3 \end{aligned}$ | This is related to different types of data structure which are playing important role for designing algorithm. |
| PCCCS404.5 | $\begin{aligned} & \text { PO1, } \\ & \text { PO2, } \\ & \text { PO3, } \\ & \text { PO4, } \\ & \text { PO8, } \\ & \text { PO9, } \\ & \text { PO10 } \end{aligned}$ | $\begin{array}{ll} 2, & 3, \\ 3, & 1, \\ 2 & 1 \end{array}$ | This CO relates to understand, analysis, design and application of the notion of Polynomial and Non-polynomial time algorithms and categorized by P, NP - Complete and NP - Hard. |
| PCCCS404.6 | $\begin{aligned} & \text { PO1, } \\ & \text { PO2, } \\ & \text { PO3, } \\ & \text { PO4, } \\ & \text { PO8, } \\ & \text { PO9, } \\ & \text { PO10 } \end{aligned}$ | $\begin{array}{lll} 2, & 3, & 2, \\ 3, & 1, & 1, \\ 2 & \end{array}$ | This CO relates to analysis of few data structures like Hash Tables, Disjoint Sets and Splay Trees where occasional operation is very slow, but most of the operations which are executing very frequently are faster. |


| CO | PSO <br> MAPP <br> ED | LEVEL | JUSTIFICATION |
| :---: | :---: | :---: | :--- |
| PCCCS404.1 | PSO1, <br> PSO2 | 2,2 | This CO is about problem analysis since it deals with correctness and <br> running time of algorithms. |
| PCCCS404.2 | PSO1, <br> PSO2 | 2,2 | This CO talks about state of the art algorithm design to develop efficient <br> algorithm. |
| PCCCS404.3 | PSO1, <br> PSO2 | 2,2 | This CO talks about state of the art Graph algorithm is required for <br> computer vision and embedded system development. |
| PCCCS404.4 | PSO1, <br> PSO2 | 2,2 | This CO talks about state of the art Data Structure is required to design <br> algorithms. |
| PCCCS404.5 | PSO1, <br> PSO2 | 2,2 | This CO talks about different categories of problems P, NP - Complete and <br> NP - Hard which is required for advance algorithms. |


| PCCCS404.6 | PSO1, <br> PSO2 | 2,2 | This CO talks about Amortized analysis which is required for few data <br> structures like Hash Tables, Disjoint Sets and Splay Trees where <br> occasional operation is very slow, but most of the operations which are <br> executing very frequently are faster. |
| :--- | :---: | :---: | :--- |

# Design \& Analysis of Algorithm MAKAUT Syllabus 

Code: PCC-CS404
Contact: 3L + 1T
Credits: 4

## Complexity Analysis:[2L]

Time and Space Complexity, Different Asymptotic notations - their mathematical significance Algortihm Design Techniques:
Divide and Conquer: [3L]
Basic method, use, Examples - Binary Search, Merge Sort, Quick Sort and their complexity.
Heap Sort and its complexity [1L]
Dynamic Programming: [3L]
Basic method, use, Examples - Matrix Chain Manipulation, All pair shortest paths, single source shortest path.
Backtracking: [2L]
Basic method, use, Examples - 8 queens problem, Graph coloring problem.
Greedy Method: [3L]
Basic method, use, Examples - Knapsack problem, Job sequencing with deadlines, Minimum cost spanning ree by Prim's and Kruskal's algorithm.
Lower Bound Theory: [1L]
O(nlgn) bound for comparison sort
Disjoint set manipulation: [2L]
Set manipulation algorithm like UNION-FIND, union by rank.
Graph traversal algorithm: Recapitulation [1L]
Breadth First Search(BFS) and Depth First Search(DFS) - Classification of edges - tree, forward, back
and cross edges - complexity and comparison
String matching problem: [3L]
Different techniques - Naive algorithm, string matching using finite automata, and Knuth, Morris, Pratt their complexities.
Amortized Analysis: [3L]
Aggregate, Accounting, and Potential Method.
Network Flow: [3L]
Ford Fulkerson algorithm, Max-Flow Min-Cut theorem (Statement and Illustration)
Matrix Manipulation Algorithm: [3L]
Strassen's matrix manipulation algorithm; application of matrix multiplication to solution of simultaneous linear equations using LUP decomposition, Inversion of matrix and Boolean matrix multiplication.
Notion of NP-completeness: [3L]
P class, NP class, NP hard class, NP complete class - their interrelationship, Satisfiability problem, Cook's theorem (Statement only), Clique decision problem

## Approximation Algorithms: [3L]

Necessity of approximation scheme, performance guarantee, polynomial time approximation schemes, vertex cover problem, travelling salesman problem.

## Text Book:

1. T. H. Cormen, C. E. Leiserson, R. L. Rivest and C. Stein, "Introduction to Algorithms"
2. A. Aho, J.Hopcroft and J.Ullman "The Design and Analysis of Algorithms"
3. D.E.Knuth "The Art of Computer Programming", Vol. 3
4. Jon Kleiberg and Eva Tardos, "Algorithm Design"

Reference:
K.Mehlhorn , "Data Structures and Algorithms" - Vol. I \& Vol. 2.
S.Baase "Computer Algorithms"
E.Horowitz and Shani "Fundamentals of Computer Algorithms"
E.M.Reingold, J.Nievergelt and N.Deo- "Combinational Algorithms- Theory and Practice", Prentice Hall, 1997

## LESSON PLAN

## Course: Design and Analysis of Algorithms

## Code: PCC-CS404

Contact: 3L
Credits: 3

## Required Text Books:

1. T. H. Cormen, C. E. Leiserson, R. L. Rivest and C. Stein, "Introduction to Algorithms" $2^{\text {nd }}$ Edition
2. E.Horowitz and Shani "Fundamentals of Computer Algorithms" ${ }^{\text {nd }}$ Edition.
3. A. Aho, J.Hopcroft and J.Ullman "The Design and Analysis of Algorithms"
4. Klenberg, Trados , "Algorithm Design"
5. Goodrich "Design of Algorithms"
6. E.M.Reingold, J.Nievergelt and N.Deo- "Combinational Algorithms- Theory and Practice", Prentice Hall, 1997

## Web resources

W1: https://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-006-introduction-to-algorithms-spring-2008/lecture-notes/

W2: https://www2.cs.duke.edu/courses/fall10/cps130/lectures.html
W3: https://www.isical.ac.in/~arijit/courses/spring2017/daa-mtech.html
W4: http://www.cs.umd.edu/class/fall2015/cmsc451/
W5: http://www.cse.iitd.ernet.in/~ssen/csl356/admin356.html
W6: https://www.cs.virginia.edu/~luebke/cs332/

W7: https://www.cs.umd.edu/users/samir/
$\begin{array}{|l|c|l|l|l|}\hline \begin{array}{c}\text { Lecture } \\ \text { No. }\end{array} & \text { Topics to be covered } & \text { Ref } & \begin{array}{c}\text { Teaching } \\ \text { Aids }\end{array} & \begin{array}{c}\text { Teaching } \\ \text { Method }\end{array} \\ \hline 1 & \begin{array}{c}\text { Course Outcome for the course CS-501; } \\ \text { Algorithm: Definition, Time and Space } \\ \text { complexity of an Algorithm, Tower of } \\ \text { Hanoi problem. }\end{array} & 1 & \begin{array}{l}\text { White } \\ \text { Board }\end{array} & \text { Discussion } \\ \hline 2 & \begin{array}{c}\text { Different Asymptotic notations: Big-O, } \\ \text { Big- } \Omega \text { (Big-Omega),Big- } \theta \text { (Big-Theta) } \\ \text { notation their mathematical significance }\end{array} & 1 & \begin{array}{l}\text { White } \\ \text { Board }\end{array} & \begin{array}{l}\text { Illustration by } \\ \text { example, } \\ \text { Discussion }\end{array} \\ \hline 3 & \begin{array}{c}\text { Introduction to divide and conquer; Binary } \\ \text { Search Algorithm: complexity analysis }\end{array} & 1 & \begin{array}{l}\text { White } \\ \text { Board }\end{array} & \begin{array}{l}\text { Illustration by } \\ \text { example, } \\ \text { Discussion }\end{array} \\ \hline \text { T1 } & \text { Analysis of Asymptotic running time of } \\ \text { Binary Search }\end{array} \quad$ W1 $\left.\quad \begin{array}{l}\text { White } \\ \text { Board }\end{array}\right]$

|  | analysis. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| T2 | Analysis of Mergesort, Quicksort and Heapsort | W3 | White Board | Illustration by example, Discussion |
| 7 | Matrix Chain Multiplication:Algorithm, Overlapping Subproblem, Optimal Substructure | 1,2 | White Board | Quiz Group discussion |
| 8 | All pair shortest path using Dynamic Programming- Floyd Warshall algorithm | 1,2 | White Board | Flip Class |
| 9 | Single source shortest path using Dynamic Programming- Bellman Ford Algorithm | 1,2 | White <br> Board PPT | Discussion |
| T3 | Discuss Floyd Warshall, Bellman Ford | W5 | White Board | Discussion |
| 10 | Backtracking: Introduction, N-Queen's problem, Solution Strategy | 2 | White Board PPT | Discussion, Surprise Test |
| 11 | Graph Coloring problem: Solution using Backtracking | 1 | White Board | Problem Solving |
| 12 | Greedy Method: Fractional Knapsack Problem- problem statement, solution | 1,2 | White Board | Problem Solving |
| T4 | Dijkstra's Algorithm | 2 | White Board | Group Discussion |
| 13 | Job Sequencing with deadlines- Greedy solution | 1,2 | White Board | Assignments |
| 14 | Minimal Spanning Tree: Prim's Algorithm \& Kruskal's algorithm | 1,2 | White Board | Discussion |
| 15 | Lower bound of comparison based sorting algorithm $\Omega(n \log n)$ | 1 | White Board | Group <br> Discussion <br> Quiz |
| T5 | Explain MST problem, Job sequencing with deadline | W1 | White Board | Quiz |
| 16 | Set manipulation algorithm UNION-FIND, Union by Rank | 2 | White Board | Flip Class |
| 17 | Graph Traversal algorithm BFS, finding shortest path and connected components | 1 | White Board | Illustration by example, Discussion |
| 18 | DFS algorithm, Edge classification in DFS Tree, Topological Sorting | 1 | White Board | Assignments |
| T6 | Explain Set manipulation , BFS and DFS algorithms | W5 | White Board | Illustration by example, Discussion |
| 19 | String Matching with Naïve algorithm | 1 | White Board | Group Discussion |
| 20 | String Matching using Finite Automata | 1 | White Board | Assignments |
| 21 | Knuth, Morris, Pratt (KMP) Algorithm | 1 | White Board | Quiz |
| T7 | Discuss String matching Algorithms | W1 | White Board | Illustration by example, Discussion |
| 22 | Aggregate method | 1, 4, 5 | White Board | Discussion |
| 23 | Accounting method | 4, 5 | White Board | Discussion |
| 24 | Potential method | 4, 5 | White Board | Discussion |
| T8 | Explain Aggregate, Accounting, Potential | W4 | White |  |
|  | Methods |  | Board |  |


| 25 | Ford - Fulkerson algorithm | 1 | PPT | Illustration by example, Discussion |
| :---: | :---: | :---: | :---: | :---: |
| 26 | Max-Flow Min-Cut Theorem | 1 | White Board | Problem Solving |
| 27 | Strassen's matrix multiplication algorithm, | 1 | White Board | Assignments |
| T9 | Explain Max-Flow Min-cut theorem with Ford Fulkerson algorithm | W3 | White Board | Illustration by example, Discussion |
| 28 | Solving linear equation using LUP Decomposition | 1 | White Board | Discussion |
| 29 | Inversion of Matrix and Boolean Matrix | 1 | White Board | Quiz |
| 30 | P Class, NP Class, NP Hard and NP Complete - inter relationship | 1 | PPT | Group <br> Discussion Quiz |
| T10 | Discuss the relation of P, NP, NP-Hard | W5 | White Board | Group Discussion |
| 31 | Satisfiability problem | 1 | PPT | Discussion |
| 32 | Cook's Theorem, Clique decision problem | 1 | White Board | Assignments |
| 33 | Necessity of approximation scheme, performance guarantee | 1 | White Board | Group <br> Discussion <br> Quiz |
| T11 | Discuss Satisfiability Problem | W3 | White Board | Discussion, Quiz |
| 34 | Polynomial time approximation schemes | 1 | White Board | Group <br> Discussion <br> Quiz |
| 35 | Vertex cover problem, Travelling Salesman problem. | 1 | White Board | Group Discussion |
| T12 | Discuss Travelling Salesman Problem and Vertex Cover Problem | W1 | White Board | Illustration by example, Discussion |
| 36 | Branch and Bound Method of solving combinatorial optimization problem solving* |  | White Board | Illustration by example, Discussion |

## ASSIGNMENT-I

OUTCOME BASED EDUCATION (OBE)

| Question No. | Knowledge Domain | Allotted Marks | COs |
| :---: | :---: | :---: | :---: |
| $1,2,3,4,6$ | Understand, Analyze |  | CO1,CO2 |
| 8,9 | Understand, Apply | 10 | $\mathrm{CO} 2, \mathrm{CO} 3, \mathrm{CO} 4$ |
| 10 | Analyze, Evaluate |  | CO |
| nnnn | Evaluate |  | CO 2 |

1. Using Recurrence Relation calculate the time complexity of

Merge Sort algorithm, Tower of Hanoi problem.
2. Write the algorithm of Quick sort. Find the best case, worst case and average case time complexities of this algorithm.
3. Let A [ 1.. n ] be a sorted array of $n$ distinct integers. Give a divide-and-conquer algorithm that can find an index i such that $\mathrm{A}[\mathrm{i}]=\mathrm{i}($ if one exists $)$ with running time $\mathrm{O}(\log n)$.

Find out the number of inversion in an Array $A[1 . . n]$ with running time $\mathrm{O}(\mathrm{nlog} n)$. If $\mathrm{i}<\mathrm{j}$ and $\mathrm{A}[\mathrm{i}]>\mathrm{A}[\mathrm{j}]$ then
Count_Inversion++
4. What is optimal substructure property? Write the algorithm for multiplying a chain of matrices A1 to An where matrix Ai has the dimension mi-1 X mi. Also find the split points. Discuss the time complexity.
5. Find at least three feasible solution for a knapsack having capacity 100 kg for the following list of items having values and weights as shown in table

| Item | Value | Weight |
| :--- | :--- | :--- |
| I1 | 10 | 15 |
| I 2 | 20 | 25 |
| I 3 | 30 | 35 |
| I 4 | 40 | 45 |
| I 5 | 50 | 55 |

Now find the optimal solution of the problem using greedy method.
6. What do you mean by Dynamic Programming ? What is the difference between dynamic programming and Greedy method?Write the Bellman Ford Algorithm. Analyze its time complexity.
7. Write the algorithm for Heap sort. Given a list of numbers $12,8,6,5,13,9,14,15,10,7,11$; show how heap sort can be applied to sort.
8. Define spanning tree. Write Prim's algorithm to find out minimum cost spanning tree of a graph. Discuss its time complexity.
9. Write Kruskal's algorithm to find out minimum cost spanning tree of a graph. Discuss implementation techniques, and its time complexity.
10. Discuss the Different Asymptotic notations: Big-O, Big- $\Omega$ (Big-Omega),Big- $\theta$ (Big-Theta) - their mathematical significance

## MODEL Question Paper (PCCCS404)

## Group A

1. $T(n)=T(9 n / 10)+n$, then which one is true...
(a) $\mathrm{O}\left(\mathrm{n}^{1 / 2}\right)$
(b) $\mathrm{O}(\mathrm{n})$
(c) $\mathrm{O}\left(\mathrm{n}^{2}\right)$
(d) $\mathrm{O}(\mathrm{nlog} 2 \mathrm{n})$
2. Choose the correct one:
I. $2^{\mathrm{n}+10}=\mathrm{O}\left(2^{\mathrm{n}}\right)$
II. $2^{10 \mathrm{n}}=\mathrm{O}\left(2^{\mathrm{n}}\right)$
(a) I Only
(b) II Only
(c) I and II
(d) None
3. $\mathrm{T}(\mathrm{n})=$ Running Time of Merge Sort. Choose the correct one...
(a) $6 n \log 2 n+6 n$
(b) $(4 n+2)(\log 2 n+1)$
(c) $\mathrm{O}(\mathrm{nlog} 2 \mathrm{n})$
(d) All of the above
4. Which of the following algorithm design techniques is used in Quick sort algorithm?
(a) Dynamic Programming (b) Backtracking
(c)
Divide and conquer(d)Greedy method
5. Time complexity of Heap sort on $n$ items is:
(a) $\mathrm{O}(\mathrm{n})$
(b) $\mathrm{O}(\mathrm{n} \log \mathrm{n})$
(c) $\mathrm{O}\left(\mathrm{n}^{2}\right)$
(d) $\mathrm{O}(\log n)$
6.In which sorting technique, an element is placed in its proper position in each step...
A. heap sort
B. bubble sort
C. quick sort
D. merge sort
6. Which of the following can not be performed recursively
(a) DFS
(b) quick sort
(c) binary search
(d)None of these
7. The time complexity of TSP is
(a) $\mathrm{O}\left(\mathrm{n}^{2} 2^{n}\right)$
(b) $\Theta\left(n^{2} 2^{n}\right)$
(c) $\Omega\left(n^{2} 2^{n}\right)$
(d)None of these
9.Which of the following algorithm solves All pair shortest path problem
(a)Dijkstra
(b)Floyd Warshall
(c) Prim's
(d)D. Kruskal'
8. Which of the following algorithm has tail recursion?
(a)Bubble sort (b)quick sort
(c)merge sort (d)none

## Group B

1. State Master Theorem and find out the complexity of the following recurrence.

$$
T(n)=2 T\left(n^{1 / 2}\right)+\log n
$$

2. Let $\mathrm{A}[1 \ldots \mathrm{n}]$ be a sorted array of n distinct integers. Give a divide and conquer algorithm which can find an index i such that $\mathrm{A}[\mathrm{i}]=\mathrm{i}$ (if one exist) with running time O(log n). 5
3. Find the minimum number of operations required for the following matrix chain multiplication using Dynamic programming: A (10 x 20) * B (20 x 50) * C (50 x 1) * D (1 x 100)

## Group C

1.(a) Explain the time complexity of Quick Sort.
(b) Implement a algorithm in $\mathrm{O}(\mathrm{nlog} \mathrm{n})$ time which will count the number of inversion in an array of integers $\mathrm{A}[10]$. The inversion will be counted If $\mathrm{i}<\mathrm{j}$ and $\mathrm{A}[\mathrm{i}]>\mathrm{A}[\mathrm{j}]$ Then count++.
(c) How Partition function of Quick Sort used to find kth smallest number in $\mathrm{O}(\log \mathrm{n})$ time.

$$
5+4+6
$$

2.(a) Write the greedy algorithm for job sequencing with deadline. Using greedy method ,find an optimal solution to the problem of job sequencing with deadline where $\mathrm{n}=4$, (p1,p2,p3,p4)=(100,10,5,27) and (d1,d2,d3,d4)=(2,1,2,1).
(b) Define spanning tree. Using prims algorithm generate the MST from the following graph. $(4+5)+(2+4)$

3. (a) Define a Graph. How shortest path is computed using BFS(Breath First Search) .
(b) Write DFS algorithm, and explain the edge classification in DFS tree with the following example.
(c) How to find that a particular graph is a DAG (Directed Acyclic Graph)

$$
(1+4)+(2+5)+4
$$



